

Figure 3:  $R_{34}$  measured (solid line) and modeled (dashed line) for all BPMs.

The very good agreement (especially in the FF) for most of the BPMs gave us good confidence in the modeling of the beamline. The precision is not as good where there were too large amplitudes because of saturation in BPM readings.

## RELATIVE ORBIT RECONSTRUCTION

### Reconstruction of parameters at injection

The reconstruction was then tried on 500 BPM readings, changing the energy by varying the frequency of the ring cavity. The  $x$ ,  $x'$ ,  $y$ ,  $y'$ ,  $dE/E$  parameters at the injection point were fitted by least square minimisation solving Equation 1. Results for the horizontal plane are shown in Figure 4.

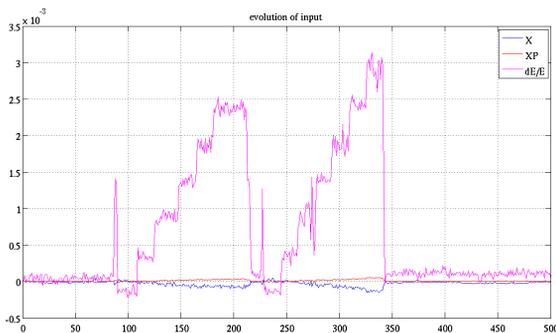


Figure 4: Evolution of  $x$ ,  $x'$  and  $dE/E$  reconstructed at the injection point.

One can clearly see that the steps in energy are well reconstructed. Also a correlation between  $x$  and  $dE/E$  and between  $x'$  and  $dE/E$  is visible, indicating some anomalous dispersion at that point.

In the vertical plane, natural fluctuations of the beam being 10x lower than in horizontal, reconstruction was not successful.

### Scale factor determinations

The reconstructed orbit deduced from these parameters is then compared to the measurements to obtain scale factors in BPM readings by a linear fit (see Figure 5).

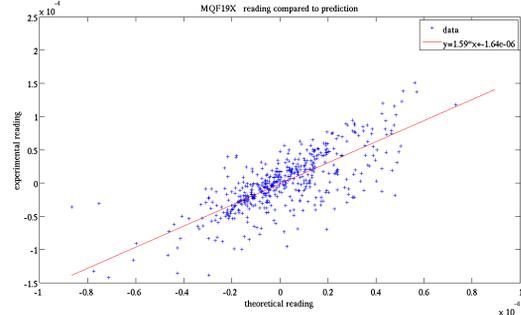


Figure 5: Example of scale factor fit. Horizontal and vertical axes show the reconstructed and experimental readings, respectively.

Horizontal scale factors of all BPMs obtained in this way are shown in Figure 6.

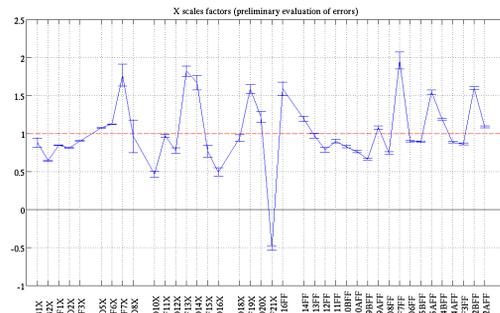


Figure 6: Horizontal scale factors of all BPMs, with estimated errors from the fit.

This estimation can be biased by an overall scale factor common to all BPMs, and should be calibrated, thanks to the energy fit or the transfer matrix measurements.

Most BPMs have scale factors between 0.75 and 1.5.

To evaluate the quality of the fit, the spread of residuals is computed for each BPM, with or without correcting for the scale factors, and compared to the initial spread of the BPM readings (see Figure 7).

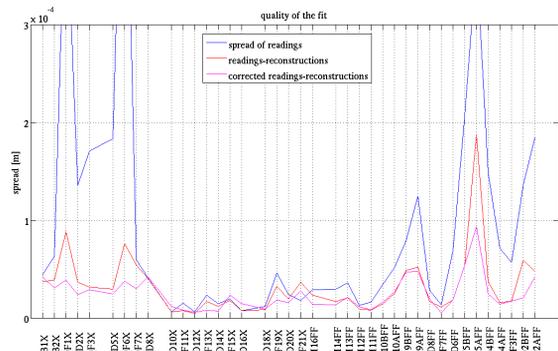


Figure 7: Spread of initial measurements and of the residuals to the reconstruction, with and without correction for scale factor.

For almost all BPMs, the spread of the residuals of the reconstruction is significantly smaller than the spread of the measurements.

It is especially true in the first part of the line where the dispersion function is large. That is a very good indication that the energy is well reconstructed.

One can also see a good reconstruction of  $x$  and  $x'$  at the end of the line where the the beta functions become very large, which is, this time, due to a good reconstruction of the positions at that location.

For the BPMs with non-unitary scale factors, the spread is further reduced when the reading is corrected by the found scale factor.

## CONCLUSION AND PROSPECTS

It was shown that the modeling of ATF2 is reliable, allowing successful reconstruction of the horizontal positions, angles and of the energy at the injection point.

Thanks to this reconstruction, one can estimate parasitically, with just beam fluctuations, the scale factors of the BPMs.

Nevertheless, because the reconstruction suffers from the bad resolutions of the first BPMs, work is on-going on their electronics, trying to improve it. That, combined with a reconstruction optimized to exploit the sub-micron resolution of the last BPMs, should allow us to reconstruct as well the vertical plane.

## REFERENCES

- [1] ATF2 Proposal, Vol 1 & 2. ATF2 Collaboration, August 11 2005 and 13 February 2006, <http://lcdev.kek.jp/ATF2/proposal>
- [2] Status report of ILC Final Focuss test beamline at ATF, Bobuhiro Terunuma, contribution to this conference